

## Pre-Calculus 11

7.2

### Multiplying & Dividing Rational Expressions.



Steps for multiplying & dividing rational expressions:

- ① When dividing, multiply by the reciprocal
- ② Factor the numerators & denominators
- ③ State restrictions (NPVs)
- ④ Cancel common factors.
- ⑤ Express answer as one rational.

Examples // Simplify each expression

$$1 \quad a) \frac{b}{4y^2} \times \frac{3a}{2b} \xrightarrow{\text{option 2:}} \frac{3ab}{24b^2} = \frac{a}{8b}, b \neq 0$$

$$b) \frac{6m^2(n+1)}{5\sqrt{m}(n-1)} \times \frac{2(n-1)}{m n}$$

$$= \frac{4m(n+1)}{5n}$$

NPVs:  $n \neq 0, n \neq 1, m \neq 0$

$$2 \quad a) \frac{12x^2}{15} \div \frac{3x}{2y} \xrightarrow{\downarrow}$$

$$= \frac{12x^2}{15} \times \frac{2y}{3x}$$

$$= \frac{8xy}{15}$$

$$c) \frac{14(m-1)}{15m^2} \div \frac{m(m-1)}{5(m+2)} \xrightarrow{\downarrow}$$

$$= \frac{14(m-1)}{15m^2} \times \frac{5(m+2)}{m(m-1)}$$

$$= \frac{14(m+2)}{3m^3}$$

NPVs:  $y \neq 0, x \neq 0$

NPVs:  $m \neq 0, m \neq 1, m \neq -2$

3. Simplify

$$a) \frac{x^2+7x+12}{x^2+2x-15} \cdot \frac{x^2-5x+6}{x^2-16}$$

$$= \frac{(x+4)(x+3)}{(x+5)(x-3)} \cdot \frac{(x-3)(x-2)}{(x-4)(x+4)}$$

$$= \frac{(x+3)(x-2)}{(x+5)(x-4)}$$

NPVs:

$$x+5 \neq 0$$

$$x-3 \neq 0$$

$$x \neq -5$$

$$x \neq 3$$

$$x+4 \neq 0 \quad x-4 \neq 0$$

$$x \neq -4$$

$$x \neq 4$$

$$b) \frac{x^2+15x+56}{x^2-3x-54} \div \frac{x^2+6x-16}{x^2+4x-12}$$

$$= \frac{x^2+15x+56}{x^2-3x-54} \times \frac{x^2+4x-12}{x^2+6x-16}$$

\*NOTE: NPV's are found from all factors EVER located in the denominator!

$$= \frac{(x+8)(x+7)}{(x-9)(x+6)} \times \frac{(x+6)(x-2)}{(x+8)(x-2)}$$

$$x \neq -6 \quad x \neq 2$$

$$x \neq 2 \quad x \neq -6$$

$$x \neq -8 \quad x \neq 9$$

$$= x+7$$

$$\frac{1}{x-9} \quad \text{NPVs: } x \neq -6, x \neq -8$$

$$x \neq 2, x \neq 9$$

$$c) \frac{12m^2-3}{2mn^2-2m^2n} \div \frac{2m+1}{5mn-5n^2}$$

$$\rightarrow = \frac{-15(2m-1)}{2m}$$

\*NOTE:

$$\frac{12m^2-3}{(m-n)} \cdot \frac{5mn-5n^2}{2m+1}$$

$$\text{NPV's: } m \neq 0 \quad m-n \neq 0$$

$$= -1(-m+n)$$

$$n \neq 0 \quad m \neq n$$

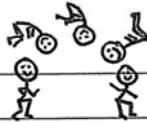
$$= -(n-m)$$

$$= \frac{3(4m^2-1)}{2mn(n-m)} \times \frac{5n(m-n)}{2m+1}$$

$$m \neq -\frac{1}{2}$$

$$= \frac{3(2m-1)(2m+1)}{2mn(n-m)} \times \frac{-5n(n-m)}{2m+1}$$

## Complex Fractions -



A complex fraction is a fraction with a fraction in the numerator and/or denominator.

### Examples //

1. Simplify the following.

$$\frac{x^2 - 4}{x+3} \rightarrow \neq 0$$
$$\frac{2x-4}{x^2+2x-3} \rightarrow \neq 0$$

$$= \frac{x^2 - 4}{x+3} \div \frac{2x-4}{x^2+2x-3}$$

$$= \frac{(x-2)(x+2)}{(x+3)} \cdot \frac{(x+3)(x-1)}{2(x-2)}$$

$$= \frac{(x+2)(x-1)}{2}$$

$$NPV_s: x \neq -3, x \neq 1, x \neq 2$$

or  $x \neq -3, 1, 2$

$$2 - \frac{6}{x}$$

$$\underline{-} \frac{1 - \frac{9}{x^2}}{x}$$

method 1: Clear The Fractions

$$\frac{(2 - \frac{6}{x}) \cdot \frac{x^2}{1}}{(1 - \frac{9}{x^2}) \cdot \frac{x^2}{1}}$$

$$= 2x^2 - \frac{6x^2}{x}$$

$$\underline{x^2 - \frac{9x^2}{x^2}}$$

$$= \frac{2x^2 - 6x}{x^2 - 9}$$

$$= \frac{2x(x-3)}{(x-3)(x+3)} = \frac{2x}{x+3}$$

NPVs:  $x \neq 3, x \neq -3$

① multiply everything by the LCD  
of the individual fractions  
(tops only)

② simplify individual fractions

③ simplify the rational

method 2: Simplify

$$\frac{2 - \frac{6}{x}}{1 - \frac{9}{x^2}}$$

① Find LCD for the numerator & denominator separately

$$\text{LCD} = x^2$$

② write over LCD

$$= \frac{\frac{2x}{x} - \frac{6}{x}}{\frac{x^2}{x^2} - \frac{9}{x^2}} = \frac{2x - 6}{x} \div \frac{x^2 - 9}{x^2} = \frac{2(x-3)}{x} \cdot \frac{x^2}{(x-3)(x+3)}$$

$$= \frac{2x}{x+3}$$

③ simplify